## **FURTHER CALCULUS**

1 Differentiate: (a) 
$$y = \frac{1}{2}x^3 - 2\cos x$$
 (b)  $y = (1 - 2x)^3$ 

2 Find 
$$\int \frac{4}{\sqrt{(1-2x)}} dx$$

3 Evaluate: (a) 
$$\int_{-1}^{0} (2x-3)^3 dx$$
 (b)  $\int_{0}^{\frac{\pi}{6}} \cos 2x dx$ 

4 Determine 
$$f'(x)$$
 when  $f(x) = \frac{1}{\sqrt[3]{(1-2x)^2}}$ 

- 5 Find the derivative of  $\cos 2x$  in two different ways.
- 6 An open top water tanker, in the shape of a triangular prism, has a capacity of 108 litres.

The tank is to be lined on the inside in order to make it watertight.

The triangular cross-section of the tank is right-angled and isosceles, with equal sides of length *x*cm.

The tank has length of *l*cm.



- (a) Show that the surface area to be lined,  $A \text{ cm}^2$ , is given by  $A(x) = x^2 + \frac{432000}{x}$ .
- (b) Find the value of *x* which minimises this surface area.