

**1** Integrate the following:

(a)  $\int (2x - 3) dx$

(b)  $\int (4 - 4x^3) dx$

(c)  $\int (x - 3)^2 dx$

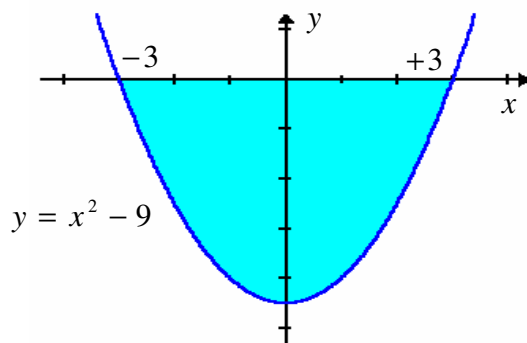
(d)  $\int \frac{x^4 + 1}{x^2} dx$

(e)  $\int \sqrt{x}(1 + \sqrt{x}) dx$

**2** Find the particular solution of the differential equation  $\frac{dy}{dx} = 2x - 1$ , given (2,8).

**3** Evaluate  $\int_{-1}^2 (3x - 1)^2 dx$

**4** The diagram below represents a bulkhead cross-section from a trawler modelled by the area between the curve  $y = x^2 - 9$  and the  $x$ -axis.



Calculate the area of the bulkhead cross-section where 1 unit = 2 metres.

**5** (a) Sketch the following pair of curves on the same diagram.

$$y = x^2 - 2x \text{ and } y = 2x$$

(b) Calculate the area of the region enclosed by the curves.

**6** Given that  $\int_0^a \sqrt[3]{x} dx = 12$ , find the value of  $a$ .