

1 Find the values of:

- (a)  $\log_9 81$     (b)  $\log_6 6$     (c)  $\log_3 1$     (d)  $\log_2 \frac{1}{4}$     (e)  $\log_{81} 9$   
 (f)  $\log_2 16 - \log_2 4$     (g)  $2\log_{10} 5 + 2\log_{10} 2$     (h)  $\frac{1}{2}\log_2 16 - \frac{1}{3}\log_2 8$

2 Solve for  $x$ , round your answers to 2 decimal places.

- (a)  $3^x = 7$     (b)  $8^x = 5$     (c)  $\ln(x) + \ln(4x) - \ln(2x) = 1$

3 Given  $\log_a 8 + \log_a 4 - \log_a 2 = 2$ , find  $a$ .

4 (a) The variables  $x$  and  $y$  are connected by a relationship of the form  $y = ax^n$ , where  $a$  and  $n$  are constants.

Show that there is a linear relationship between  $\log_{10} y$  and  $\log_{10} x$ .

(b) From an experiment some data was obtained.

The table shows the data which lies on the line of best fit.

$x$	1	4	9	16
$y$	4.0	2.0	1.3	1.0

The variables  $a$  and  $n$  in the above table are connected by a relationship of the form  $y = ax^n$ .

Determine the values of  $a$  and  $n$ .

5 The mass of a radioactive element decreases at a rate given by  $m_t = m_0 e^{-0.01t}$ , where  $t$  is the time in years.

Find:

- (a) the mass of 250mg of the element after a century,  
 (b) the half-life of the element.

